

TRANSFORMATIONS: S.G.1-8.G.4

Label each of the following as either similar or congruent.

similar A dilation with a scale factor of $\frac{1}{2}$ and a translation of 2 units horizontally.

congruent A reflection over the x-axis and a rotation of 90° clockwise.

congruent A rotation of 270° CCW followed by a reflection over the x-axis.

congruent A reflection over the y-axis followed by a reflection over the x-axis.

* Remember: only dilations lead to similarity

For each rule below, describe the transformation or sequence of transformations that took place.

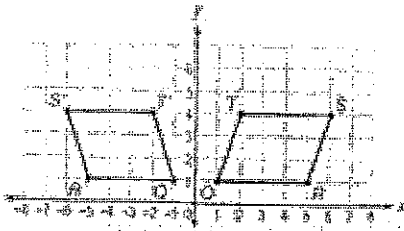
$(x,y) \rightarrow (3x,3y)$ Dilation with a scale factor of 3

$(x,y) \rightarrow (3x,3y-2)$ Dilation with a scale factor of 3 and translation 2 units down

$(x,y) \rightarrow (x+4,y-2)$ Translation 4 units right and 2 units down

$(x,y) \rightarrow (-x,y)$ Reflection over the y-axis

Parallelogram QRST is reflected over the y-axis to create parallelogram Q'R'S'T'. Use this information to answer questions 1 and 2.



1. Which angle is congruent to $\angle S$?

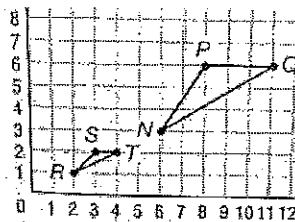
- A. $\angle Q'$
- B. $\angle R'$
- C. $\angle S'$
- D. $\angle T'$

2. \overline{QR} is parallel to \overline{TS} . Which side is parallel to $\overline{Q'R'}$?

- A. $\overline{S'R'}$
- B. $\overline{S'T'}$
- C. $\overline{Q'T'}$
- D. \overline{RS}

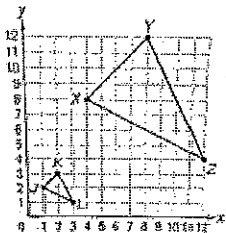
Triangle RST is the result of a dilation of $\triangle NPQ$ with the center of dilation at the origin and a scale factor of $\frac{1}{3}$. Which of the following must be true?

- A. $\angle N$ is congruent to $\angle R$.
- B. $\angle N$ is congruent to $\angle S$.
- C. $\angle P$ is congruent to $\angle R$.
- D. $\angle P$ is congruent to $\angle T$.



* Remember that angles don't change, even in a dilation.

Triangle XYZ is the result of a dilation of $\triangle JKL$ with the center of dilation at the origin and a scale factor of 4. Use this to answer questions 5 and 6.



Which names a pair of corresponding, congruent angles?

- A. $\angle L$ and $\angle X$
- B. $\angle L$ and $\angle Y$
- C. $\angle K$ and $\angle X$
- D. $\angle K$ and $\angle Y$

Which is NOT true of the triangles in the diagram?

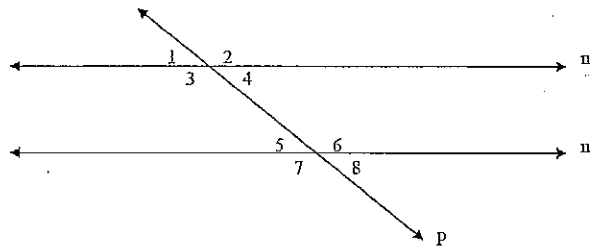
- A. $\triangle XYZ$ is similar to $\triangle JKL$ because a dilated image is similar to the original figure.
- B. The ratio of $\frac{JK}{XY}$ is equivalent to the ratio of $\frac{KL}{YZ}$.
- C. $m\angle J = m\angle X$.
- D. $JL = XZ$ (sides aren't equal in a dilation)

SPECIAL ANGLES 8.G.5

When parallel lines are cut by a transversal, they create special angle relationships. Each relationship is either congruent (equal) or supplementary (add up to 180°). You must know the relationships and if they are equal or supplementary. Study your vocabulary!

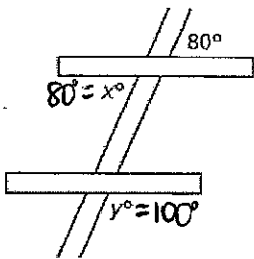
In the picture below, lines m and n are parallel and line p is a transversal.

Supplementary Angle Examples:	Congruent Angle Examples:
$\angle 1$ and $\angle 2$ form a straight line and are supplementary $\angle 1$ and $\angle 7$ are supplementary because they are same side exterior angles $\angle 3$ and $\angle 5$ are supplementary because they are same side interior angles	$\angle 1$ and $\angle 5$ are congruent because they are corresponding angles. $\angle 3$ and $\angle 6$ are congruent because they are alternate interior angles $\angle 2$ and $\angle 7$ are congruent because they are alternate exterior angles $\angle 2$ and $\angle 3$ are congruent because they are vertical angles



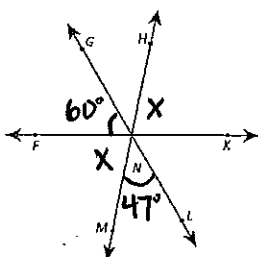
1. What relationship exist between angles 1 and 2?
 - a. Corresponding Angles
 - b. Supplementary Angles
 - c. Vertical Angles
 - d. Alternate Exterior Angles
2. What relationship exist between angles 2 and 3?
 - a. Corresponding Angles
 - b. Supplementary Angles
 - c. Vertical Angles
 - d. Alternate Exterior Angles
3. What relationship exist between angles 1 and 5?
 - a. Corresponding Angles
 - b. Supplementary Angles
 - c. Vertical Angles
 - d. Alternate Exterior Angles
4. What relationship exist between angles 2 and 7?
 - a. Corresponding Angles
 - b. Supplementary Angles
 - c. Vertical Angles
 - d. Alternate Exterior Angles

The figure below shows part of a stepladder with two steps. Each step is parallel to the ground and attached to a diagonal rod.



Which conclusion is true based on the given information and angle relationships?

- A. The value of x is 80 because vertical angles are congruent.
- B. The value of x is 80 because adjacent angles are congruent.
- C. The value of x is 100 because alternate vertical angles are supplementary.
- D. The value of x is 100 because alternate exterior angles are supplementary.



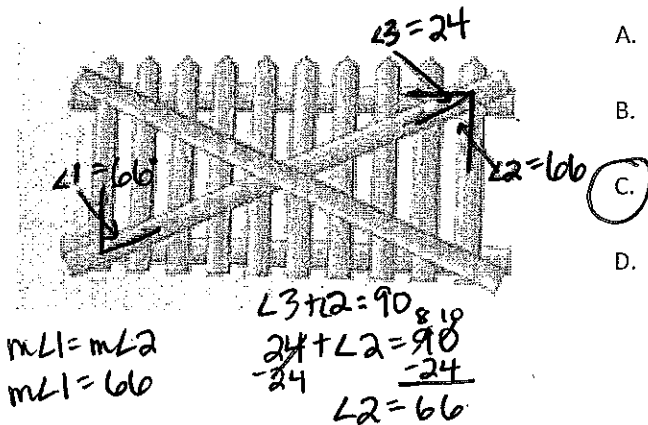
In the diagram to the left, three lines intersect at N . The measure of $\angle GNF$ is 60° , and the measure of $\angle MNL$ is 47° . What is the measure of $\angle HNK$?

$$\begin{aligned}
 60 + x + 47 &= 180 \\
 107 + x &= 180 \\
 -107 \quad -107 & \\
 x &= 73
 \end{aligned}$$

$m\angle HNK = x$ (since they're vertical angles)

$m\angle HNK = 73^\circ$

The gate for a picket fence has a cross brace as shown in the diagram below. The two horizontal braces are parallel and the measure of $\angle 3$ is 24° . Which explanation could be used to find the measure of $\angle 1$?



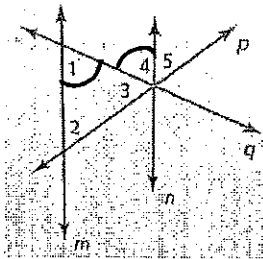
- A. Since $\angle 2$ and $\angle 3$ are complementary angles, $m\angle 2$ is 66° . $\angle 1$ and $\angle 2$ are alternate exterior angles, so $m\angle 1$ is 66° .
- B. Since $\angle 2$ and $\angle 3$ are supplementary angles, $m\angle 2$ is 156° . $\angle 1$ and $\angle 2$ are alternate interior angles, so $m\angle 1$ is 156° .
- C. Since $\angle 2$ and $\angle 3$ are complementary angles, $m\angle 2$ is 66° . $\angle 1$ and $\angle 2$ are alternate interior angles, so $m\angle 1$ is 66° .
- D. Since $\angle 2$ and $\angle 3$ are supplementary angles, $m\angle 2$ is 156° . $\angle 1$ and $\angle 2$ are corresponding angles, so $m\angle 1$ is 156° .

Triangles

1. Any angles that form a straight line are supplementary and have a sum of 180° .
2. The interior angles of a triangle have a sum of 180° .
3. An exterior angle will be equal to the sum of its remote interior angles (the two furthest away).

All of these rules are true all of the time! You can use them to solve for missing angles.

In the figure below, lines m and n are parallel. Which valid statement is part of the proof that the sum of the measures of $\angle 1$, $\angle 2$, and $\angle 3$ is 180° ?



- A. $\angle 1$ and $\angle 4$ are congruent because they are alternate interior angles on the transversal q .
- B. $\angle 1$ and $\angle 4$ are congruent because they are corresponding angles on the transversal q .
- C. $\angle 2$ and $\angle 4$ are congruent because they are alternate interior angles on the transversal q .
- D. $\angle 2$ and $\angle 4$ are supplementary because they are alternate interior angles on the transversal q .