

8.NS.2 Use rational number approximations of irrational numbers to compare the size of irrational numbers, locate them approximately on a number line diagram, and estimate the value of expressions.

What is the best approximation for $\sqrt{118}$?

- A. $11 \times 11 = 121$
- B. $10.7 \times 10.7 = 114.49$
- C. $10.9 \times 10.9 = 118.81$**
- D. $10.8 \times 10.8 = 116.64$



Which point best represents $\sqrt{55}$? Explain your answer.

- A. A** because it is about halfway between 7 and 8.
- B. B because it is a little less than 8.
- C. C because it is greater than 8.
- D. D because it is exactly 11.

Which of the following shows these numbers listed from LEAST to GREATEST?

- A. $\sqrt{64}, \pi, \sqrt{8}, 1.4, \frac{1}{2}$
 - B. $\sqrt{64}, \sqrt{8}, \frac{1}{2}, \pi, 1.4$
 - C. $\frac{1}{2}, \sqrt{8}, \sqrt{64}, 1.4, \pi$
 - D. $\frac{1}{2}, 1.4, \sqrt{8}, \pi, \sqrt{64}$**
- Handwritten notes: $\sqrt{64} = 8$, $\pi \approx 3.14$, $\sqrt{8} \approx 2.8$, 1.4 , $\frac{1}{2} = .5$

Which range contains the value of $\sqrt{(16 + 9 + 20)}$?

- A. between 6 and 7**
 - B. between 7 and 8
 - C. between 16 and 17
 - D. between 22 and 23
- Handwritten notes: $\sqrt{45}$, $6 = \sqrt{36}$, $7 = \sqrt{49}$

One of Sierra's homework problems is to evaluate the expression shown below.

$$\sqrt{19} - 3$$

Part A

Anna knows $\sqrt{19}$ is irrational. Should she expect the expression $\sqrt{19} - 3$ to be rational or irrational? Explain your answer.

Irrational! $\sqrt{19} \approx 4.358$

$$\begin{array}{r} 4.358 \\ -3 \\ \hline 1.358 \end{array}$$

 The answer would still be a non terminating non repeating decimal.

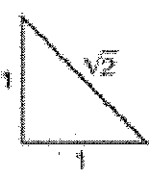
Part B

Show a sequence of steps Anna could use to determine the two consecutive numbers, counting by tenths, that the value of $\sqrt{19} - 3$ falls between. Show your work or explain your answer.

$\sqrt{19}$ is approximately 4.3. If I subtract 3, I get ≈ 1.3 which is between 1 & 2.

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The figure below is a right triangle.



Handwritten notes: $\sqrt{2}$, $\frac{11}{7} = 1.5714 \approx \sqrt{2}$, $\frac{14}{10} = 1.4$

Which is the best approximation of the hypotenuse of the right triangle?

- A. 1.21
- B. 1.41
- C. 1.73
- D. 2.24

Handwritten calculations:

$$\begin{array}{r} 1.21 \\ \times 1.21 \\ \hline 1.4641 \end{array}$$

$$\begin{array}{r} 1.41 \\ \times 1.41 \\ \hline 1.9881 \end{array}$$

A coaster in the shape of a square covers an area of 36 square centimeters. What is the length of one side of the coaster?

- A. 3 centimeters
- B. 6 centimeters
- C. 12 centimeters
- D. 18 centimeters

Handwritten calculation: $36 \sqrt{36} = 6$

Which is equivalent to $\sqrt[3]{216}$?

- A. 6
- B. 8
- C. 72
- D. 108

Which of the following is 4.58 when approximated to the nearest hundredth?

- A. $\sqrt{20}$
- B. $\sqrt{21}$
- C. $\sqrt{22}$
- D. $4\sqrt{58}$

Handwritten calculation: $\sqrt{21} \approx 4.58$

In an art class, Jorge constructs a 2 feet by 4 feet rectangular frame for a painting he just finished. He uses the Pythagorean Theorem to find the diagonal of the frame, which is $\sqrt{20}$ feet. He then concludes that the diagonal must be at least 5 feet. Is he correct in his conclusion?

- A. Yes, because $2 + 4 \leq 6$.
- B. No, because $4^2 = 16$ and $5^2 = 25$, so $\sqrt{20}$ must be between 4 and 5.
- C. Yes, because $\sqrt{20} \approx 5.48$
- D. No, because $\sqrt{20} = 2^2 + 3^2$, so $\sqrt{20}$ must be between 2 and 3.

Omar has been practicing swimming in his public pool for a swimming race. The farthest he can swim without resting is the diagonal of the pool, which is $\sqrt{200}$ meters. The three races available are the 10-meter, the 15-meter, and the 20-meter swim.

Part A: Between which two races is the length of the pool diagonal that Omar can swim? Explain your reasoning.

Handwritten calculation: $\sqrt{100} = 10$

Handwritten calculation: $\sqrt{225} = 15$

Handwritten calculation: $\sqrt{400} = 20$

Handwritten note: $\sqrt{200}$ is between 10 & 15.

Part B: In which race would Omar compete if he cannot rest during the race?

Handwritten answer: 10 meters because $\sqrt{225} > \sqrt{200}$

Part C: If, in the future, Omar can swim the length of a pool diagonal that measures $\sqrt{400}$ meters, what is the longest race he can swim without resting?

Handwritten answer: 20 meters because $\sqrt{400} = 20$