

8.F.2 Compare properties of two functions each represented in a different way.

Mattie created two functions.  $m = \frac{4}{2} = 2$  Function B

For Function A, the value of  $y$  is two less than four times the value of  $x$ . The table to the right represents Function B.

x	y
-3	-9
-1	-5
1	-1
3	3

$y = 4x - 2$

In comparing the rates of change, which statement is true?

- a) Function A and Function B have the same rate of change.
- b) Function A has a greater rate of change than Function B has.
- c) Function A and Function B both have negative rates of change.
- d) Function A has a negative rate of change and Function B has a positive rate of change.

Michelle planted two plants. After each plant had grown a little, she began using them for a science experiment.

Plant 1:

Number of Days (x)	0	1	2	3	4
Height in cm (y)	1.5	3.5	5.5	7.5	9.5

Plant 2:

The equation  $y = 3 + 1.5x$  represents  $y$ , the height in centimeters, of Plant 2 over  $x$  days.  $m = 1.5$

The correct rates of change for Plant 1 and 2 are?

- a) Plant 1 is 1.5; Plant 2 is 1.5
- b) Plant 1 is 1.0; Plant 2 is 3
- c) Plant 1 is 1.5; Plant 2 is 3
- d) Plant 1 is 2.0; Plant 2 is 1.5

Two relations are given in different formats. Use these relations to answer the questions.

Part A: Determine whether or not each relation represents a function. Justify your answers.

Both relations are functions, because each has  $x$  being paired with only one  $y$ .

Part B: Determine whether each function identified in Part A is linear or nonlinear. Explain how you know.

Relation 1 is linear, because it shows a straight line on the graph, but Relation 2 is nonlinear because it doesn't have a constant rate of change.

Part C: Write an equation for each linear function identified in Part B. Explain what each part of your equation(s) represents.  $y = -\frac{1}{5}x + 3$   $-\frac{1}{5}$  is the rate of change and 3 is the  $y$ -intercept.

Salary Plan 1

$y = 7x + 100$

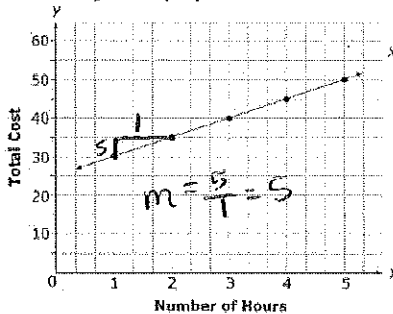
Salary Plan 2

x	y
10	152
20	252
30	352
40	452

John was given a choice between two weekly salary plans. He plans to work for one year. What information should he use to choose?

- a) He chose Plan 1 because of the \$100.
- b) He chose Plan 2 because of the \$152.
- c) He chose Plan 1 because of the \$7.
- d) He chose Plan 2 because of the \$100/10.

Kelly's Equipment Rental



Wendy's Watersports

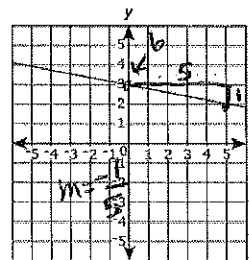
Hours	Cost
2	\$35
5	\$65
7	\$85

$m = \frac{30}{3} = 10$

The FFA leader was trying to decide which kayak rental was a better deal, which is correct?

- a) Wendy's charges \$10 less per hour.
- b) Kelly's charges \$10 less per hour.
- c) Wendy's charges \$5 less per hour.
- d) Kelly's charges \$5 less per hour.

Relation 1

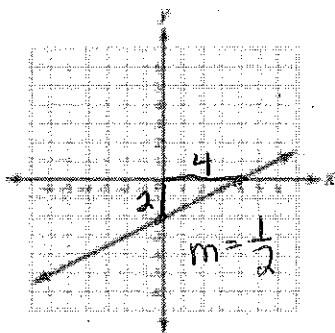


Relation 2

m	t
-3	10
-2	5
-1	2
0	1
1	2
2	5
3	10

**8.F.2 Compare properties of two functions each represented in a different way.**

The table and graph below represent two functions.



Function B	
x	y
-5	1.75
-2	2.5
0	3
4	4
10	5.5

$+4 < \begin{matrix} \nearrow \\ \searrow \end{matrix} +1$   
 $m = \frac{1}{4}$

Which of the following statements is true?

- A. The rate of change for Function A is twice the rate of change for Function B.
- B. The rate of change for Function A is four times the rate of change for Function B.
- C. The rate of change for Function B is twice the rate of change for Function A.
- D. The rate of change for Function B is one-tenth the rate of change for Function A.

Mr. Carter asked his class to compare rates of change for the functions shown below.

Function A	
x	y
-6	$-\frac{12}{5}$
-4	$-\frac{2}{5}$
0	2
2	$3\frac{1}{5}$
9	$7\frac{2}{5}$

Function B

$$y = \frac{5}{8}x + 6$$

$$m = \frac{5}{8} = 0.625$$

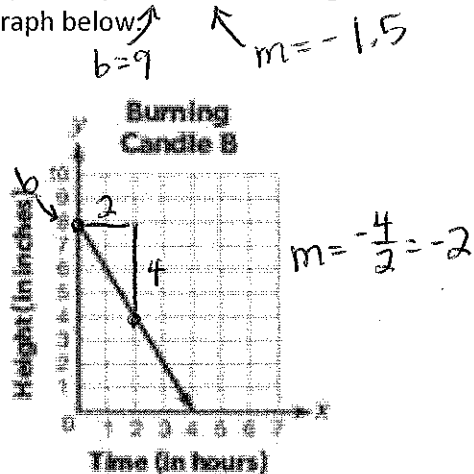
$+2 < \begin{matrix} \nearrow \\ \searrow \end{matrix} +1\frac{1}{5}$

$$m = \frac{1\frac{1}{5}}{2} = \frac{\frac{6}{5}}{2} = \frac{6}{5} \cdot \frac{1}{2} = \frac{6}{10} = \frac{3}{5} = 0.6$$

Which of the following is true?

- A. The rate of change for Function A is greater than the rate of change for Function B.
- B. The rate of change for Function B is three times greater than the rate of change for Function A.
- C. The rate of change for Function B is greater than the rate of change for Function A.
- D. The rate of change for both functions is equal.

Adam lights two candles, each a different height, at the same time and keeps track of how their heights change as they burn. The height of candle A, in inches, after it has burned  $x$  hours, is described by the equation  $y = 9 - 1.5h$ . The height of candle B, in inches, after it has burned for  $x$  hours, is shown by the graph below.



Part A: Which candle was taller before it was lit? Explain how you know.

Candle A was taller. It was 9 inches when it was lit and Candle B was 8 inches.

Part B: Which candle is burning at a faster rate? Justify using mathematical language.

Candle B is burning faster. It's burning 2 inches per hour, and candle A is burning 1.5 inches per hour.

Part C: Explain how you used the equation and the graph to determine your answers.

The 9 in the equation was Candle A's height, and the graph for Candle B showed 8 as the beginning height. The rate of change in the equation was Candle A's burning rate, and the slope from the graph was Candle B's.